

EE 109 Unit 6

Software State Machines

What is state?

- It's late at night. You see a DPS officer approaching you. Are you happy?
 - It depends on what was happening just a minute ago.
 - Your car broke down.
 - You've been partying a little too hard.
- You press the PAUSE/PLAY button on a video player. What happens?
 - It depends on what was happening previously.
 - We also want to stay in that mode indefinitely after the button is released.
 - This requires maintaining STATE, which helps us remember the necessary information for the system to operate correctly



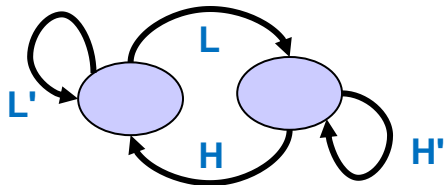
What is state?

- **State**: Everything that must be **remembered** to **interpret the inputs** (think the play/pause button) and/or to produce **outputs at appropriate times**
 - Usually, state is required for **time-dependent** behavior
- As a human:
 - Your "state" determines your interpretation of your senses and thoughts
 - The sum of all your previous experiences is what is known as state
- In a circuit:
 - State refers to all the bits being remembered in **registers** or **memory**
- In software:
 - State refers to all the **variable** values that are being used

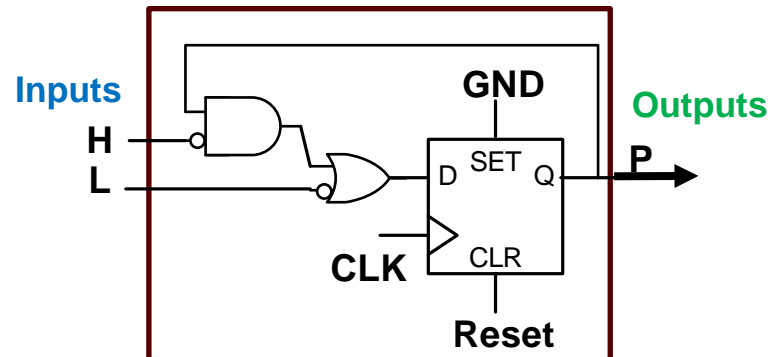
State Machines and State Diagrams

- Hardware and software components that utilize state are referred to as **state machines** (or FSMs = Finite State Machines)
- A state machine is modeled by a **state diagram** (i.e. a flow-chart)
- **FSMs are a very nice problem-solving approach/strategy**
 - If you can model your design with a state diagram, there are **straightforward transformations** to either software (what we'll study today) or hardware (later in the semester)

State Diagram
(Abstract representation of
FSM operation)

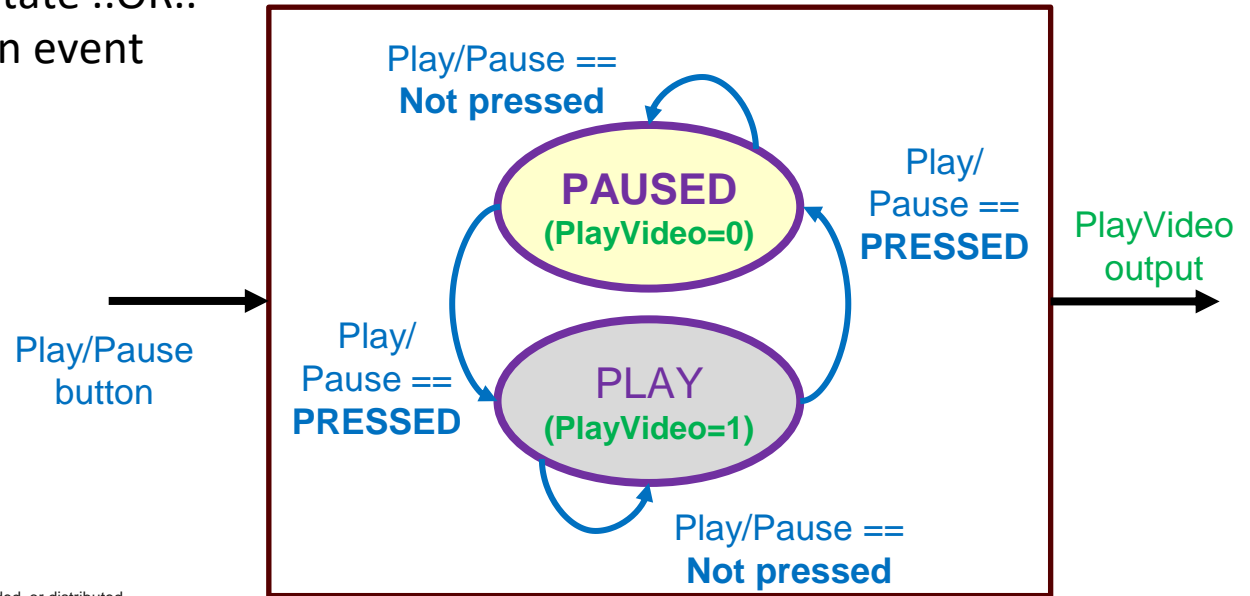


State Machine



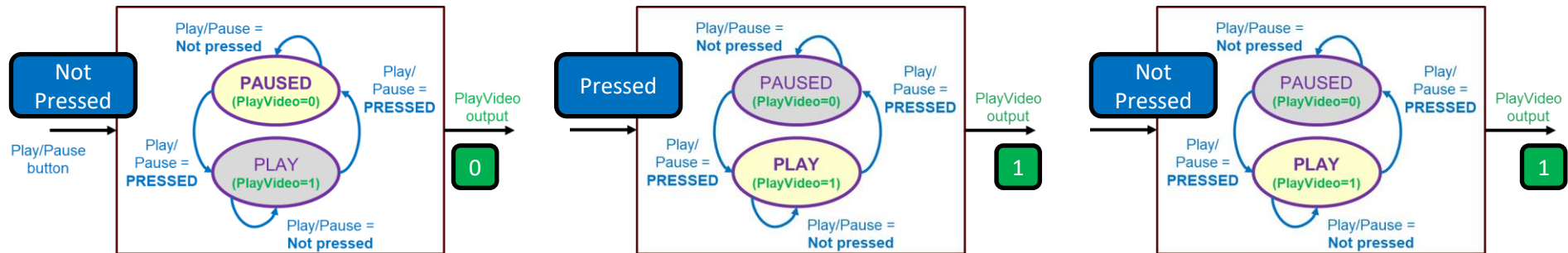
State Diagrams

- The **state diagram** should have 3 parts:
 - The **states** as circles or boxes
 - The **transitions** as arrows labeled by **input** conditions
 - The **outputs**, which can be generated when in a particular state ..OR.. on a specific transition event



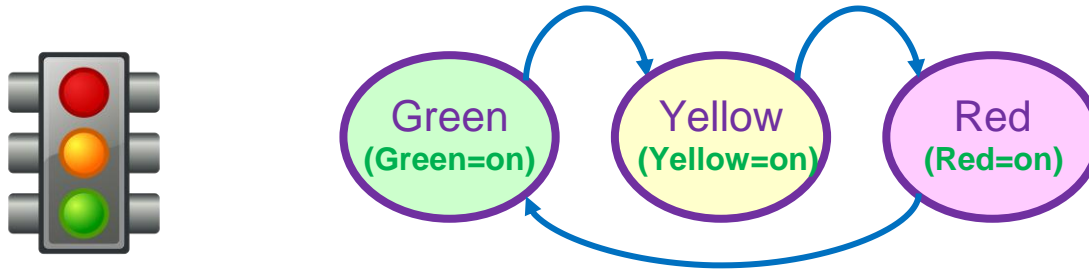
Operation

- **State** is used to generate the **outputs** even while the **inputs** are not activated
- When an **input** is activated, the **state** can be updated...
- ...and remembered after the **input** has deactivated



Another Example: Traffic Light

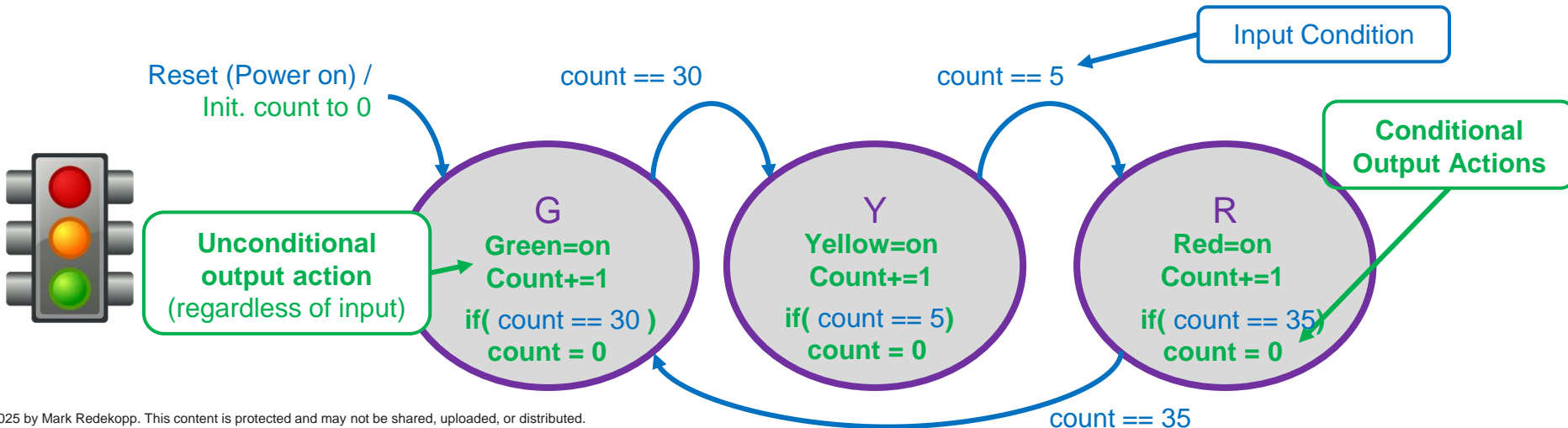
- State machines can be used to trigger **time-dependent** updates
 - Consider a system controlling the traffic lights at an intersection
 - There are no external **inputs** to indicate when the light should change
 - Instead, the **outputs** must change/transition based on time.
 - The **state** helps determine what the next **output** should be.



If a transition does not have a condition, it means it is unconditional. Sometimes we may just label it with **1 (true)**

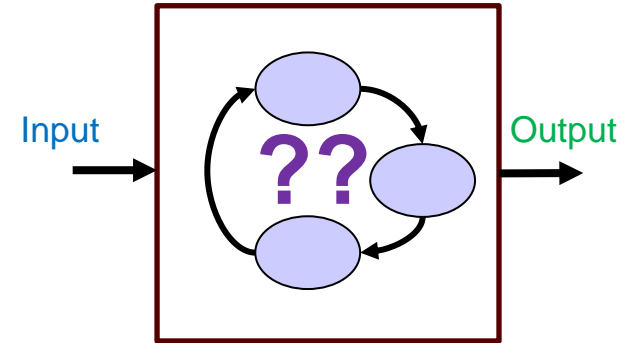
Time-Based Conditions

- Oftentimes we can use some kind of internal time counter to control when we transition states
 - Suppose our internal SW loop cycles every 1 second
- We can generate our **output/actions**
 - On each iteration, based on **state** (Green, Yellow, Red lights; increment counter)
 - On specific iterations based on other **conditions** (if count is 30, reset it to 0)



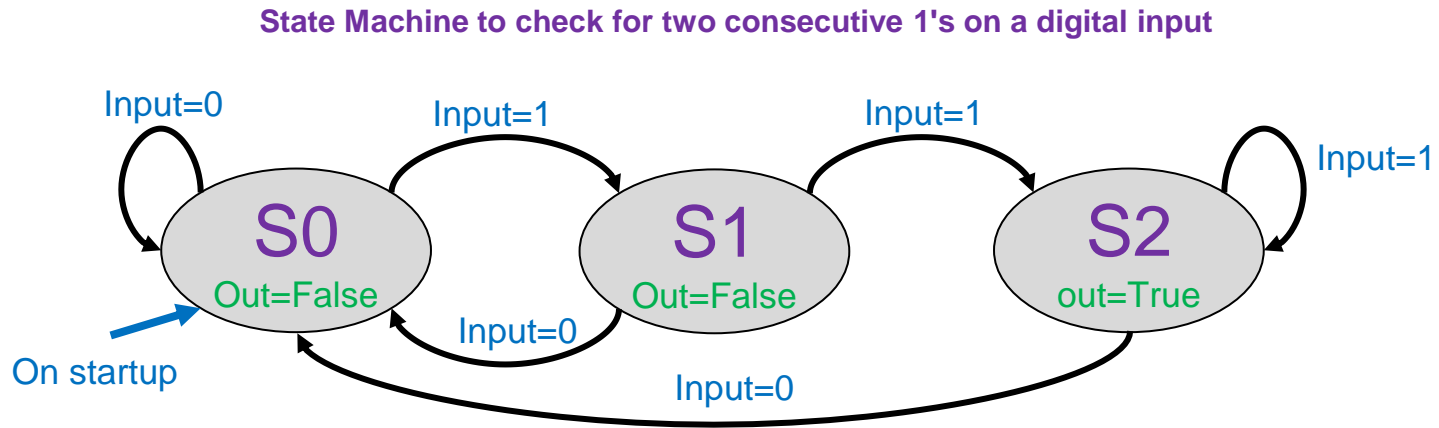
FSM Example 1-1

- Consider a system with one digital input and one output.
- The output should be true whenever the input is 1 for two consecutive time units
 - Input: 0 1 0 1 1 0 1 1 1 0
 - Output: 0 0 0 0 0 1 0 0 1 1
- Does this system need state?
- To help answer the question:
 - "The input is a 1 right now, should the output be true?"
 - Need to know whether the input was true last time unit as well? We need state!



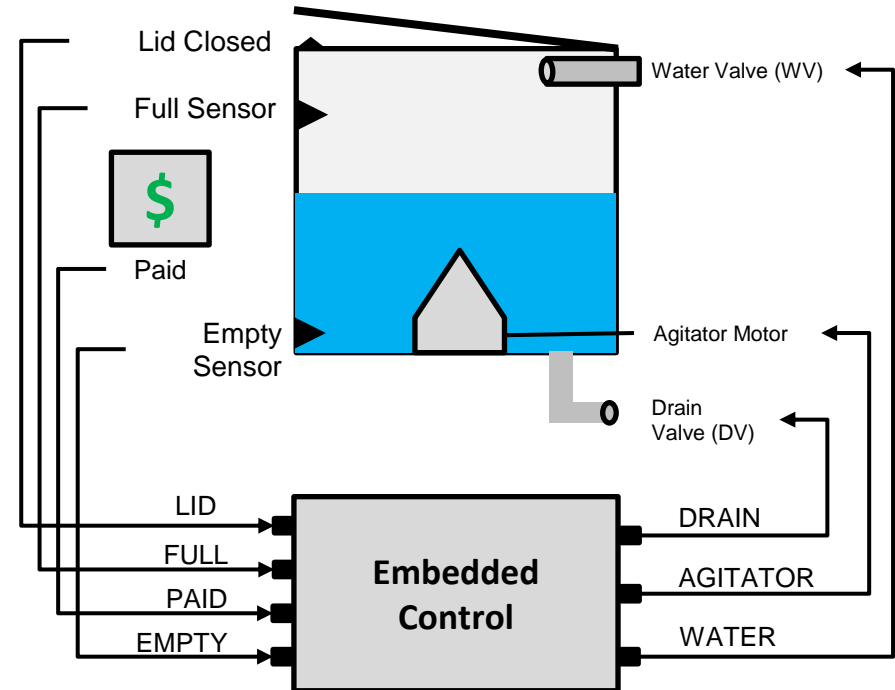
FSM Example 1-2

- Draw the state diagram for the system that outputs true (1) whenever the input has been 1 for two consecutive time periods



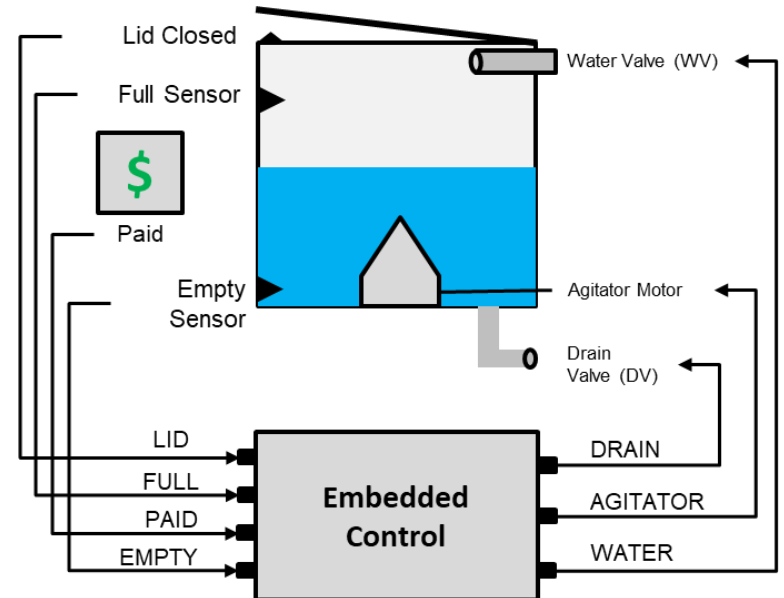
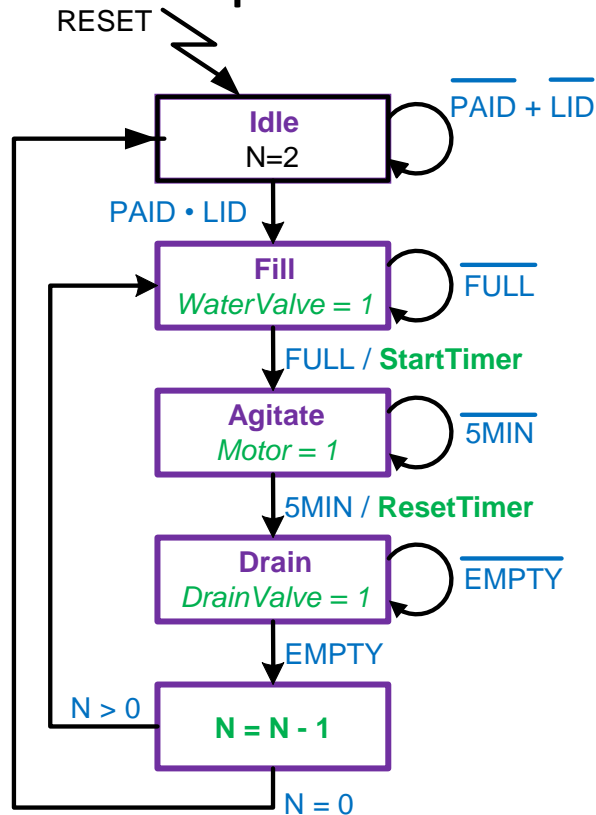
FSM Example 2: Washing Machine

- Consider the design of an embedded controller for a coin/card-operated laundry machine.
- Consider the inputs and outputs



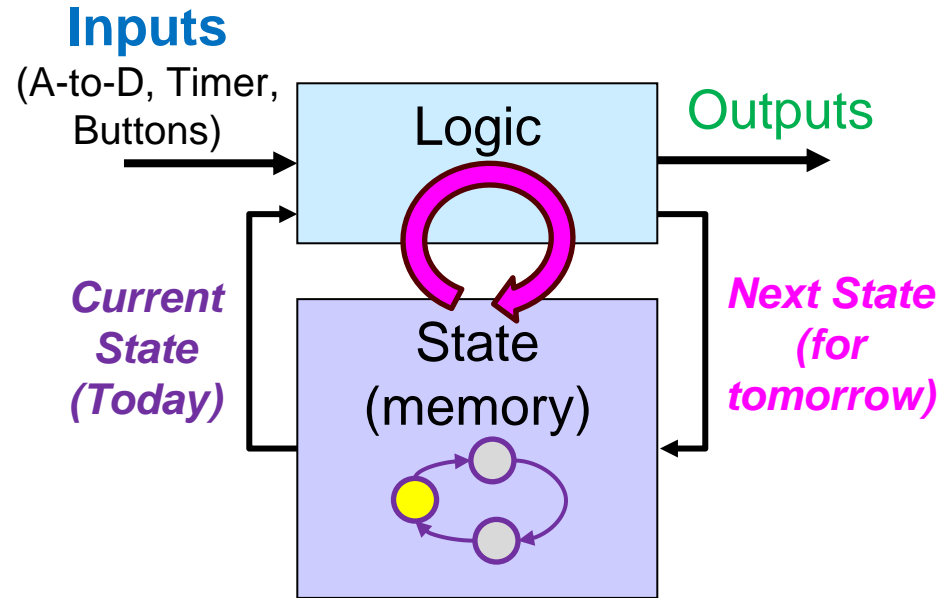
Washing Machine State Diagram

- Examine a potential state machine for this design.



A Day in the Life of a State Machine

- State machines operate time step by time step
 - **Human analogy: day-by-day (see inset)**
- Each time step, the state machine use current (today's) state to:
 - Determine which inputs to examine to determine the **next (tomorrow's) state**
 - Determine any **outputs** and **actions** to take (sometimes based on the inputs)

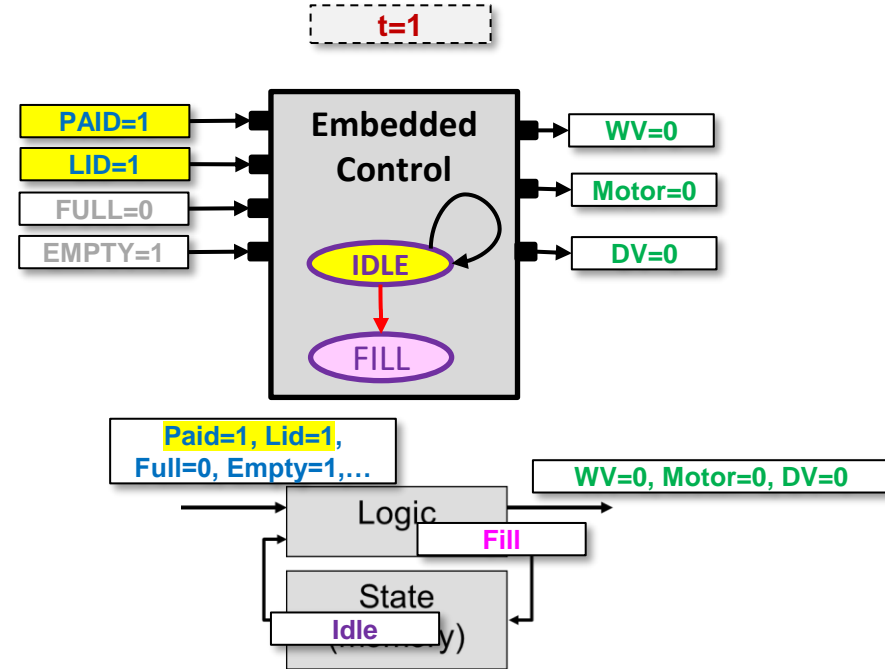
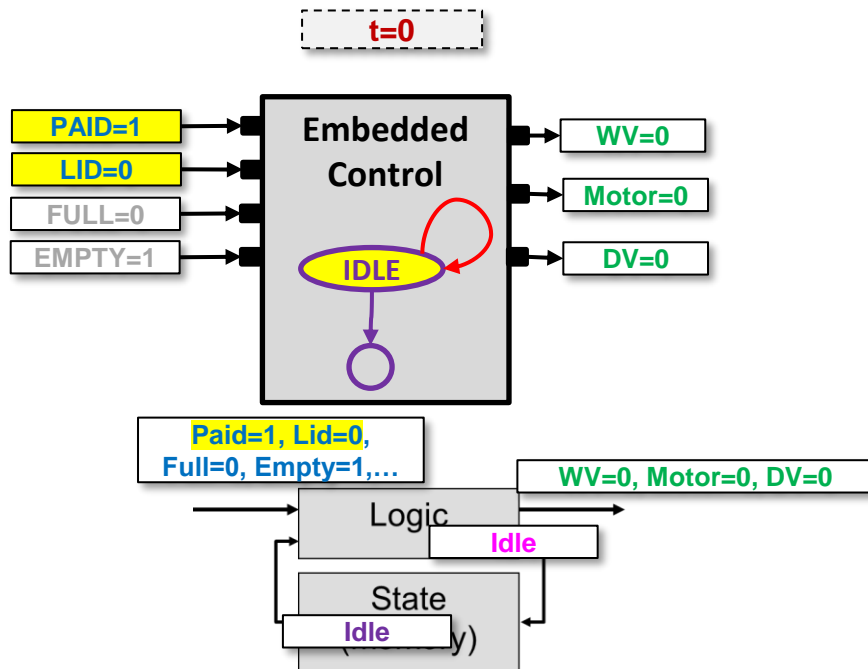
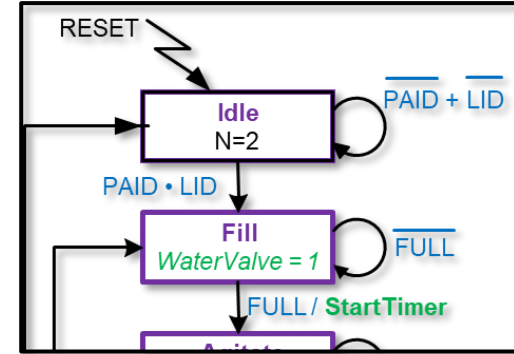


Human analogy: day-by-day

- Wake up with only a **memory** of the **current state**
- Use **current state** (and inputs) to determine **outputs** and **actions** for today
- Use **current state** and **inputs** to update state (i.e. determine state for tomorrow)
- Go to sleep and repeat same process tomorrow

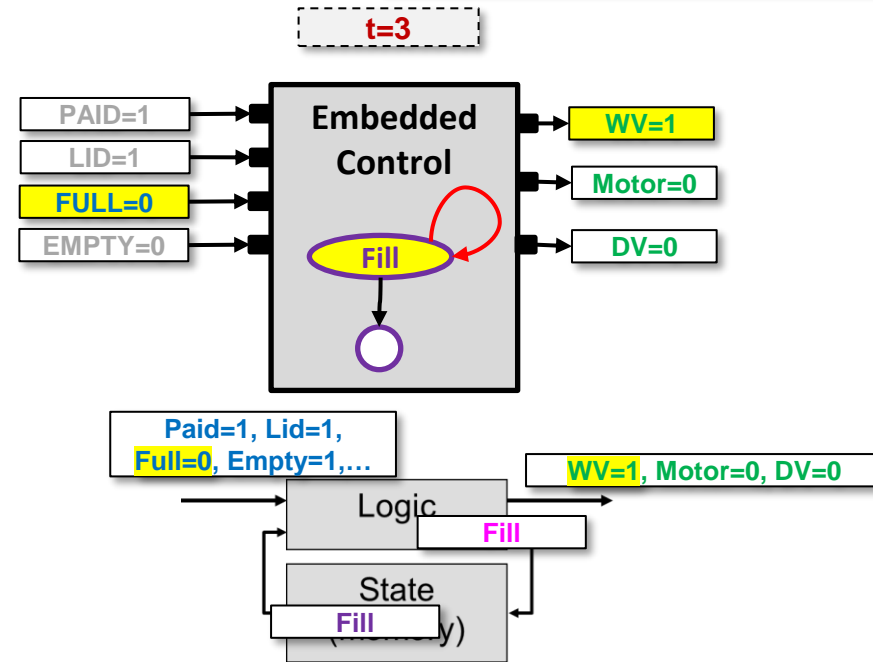
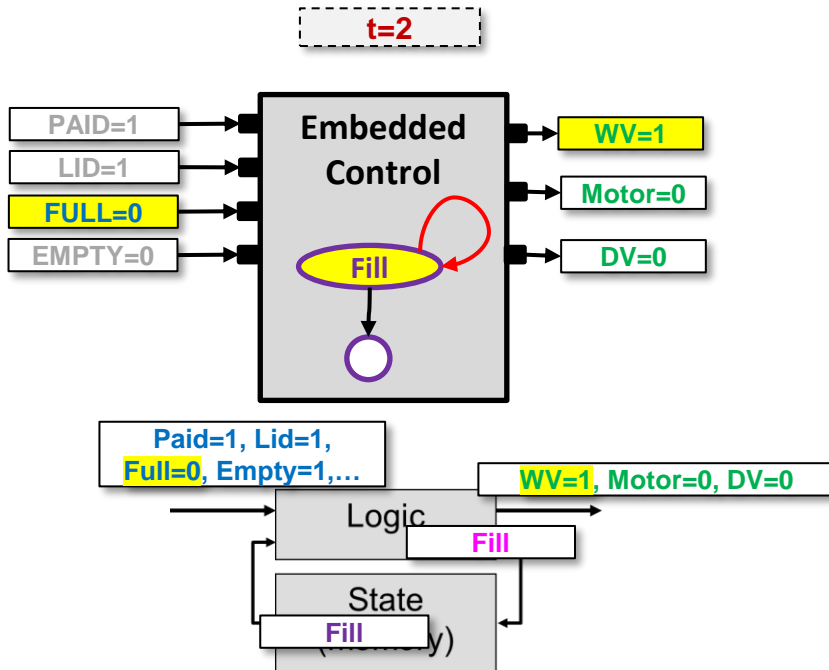
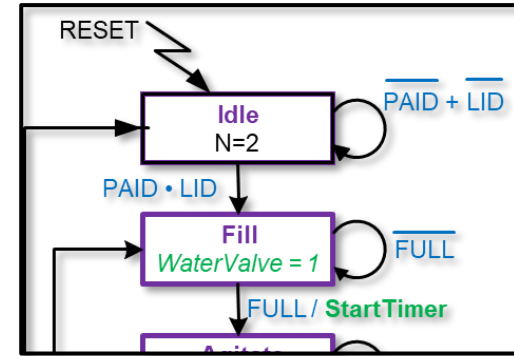
State Machine Operation (1)

- Notice how the current state helps identify which inputs "matter" at specific times



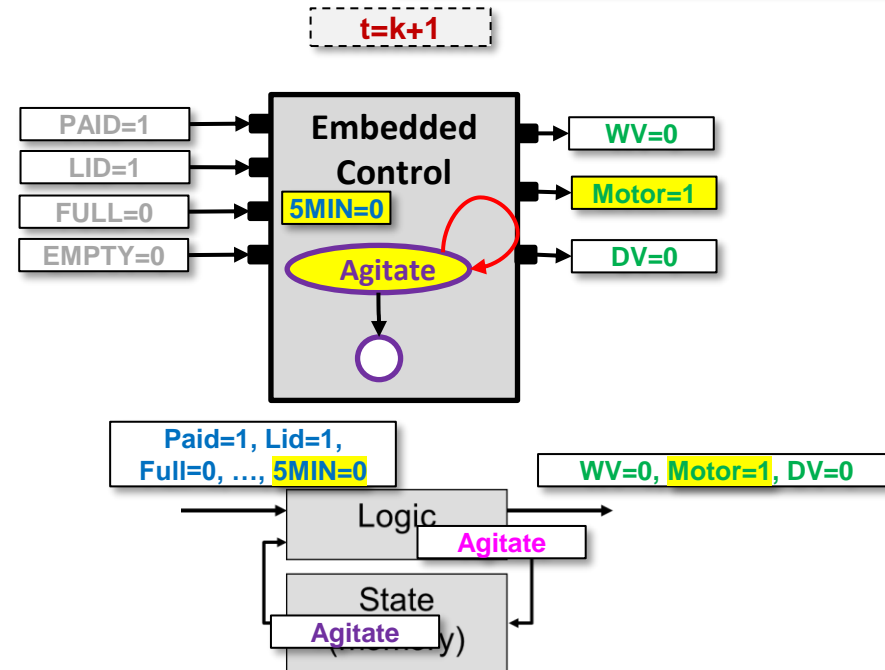
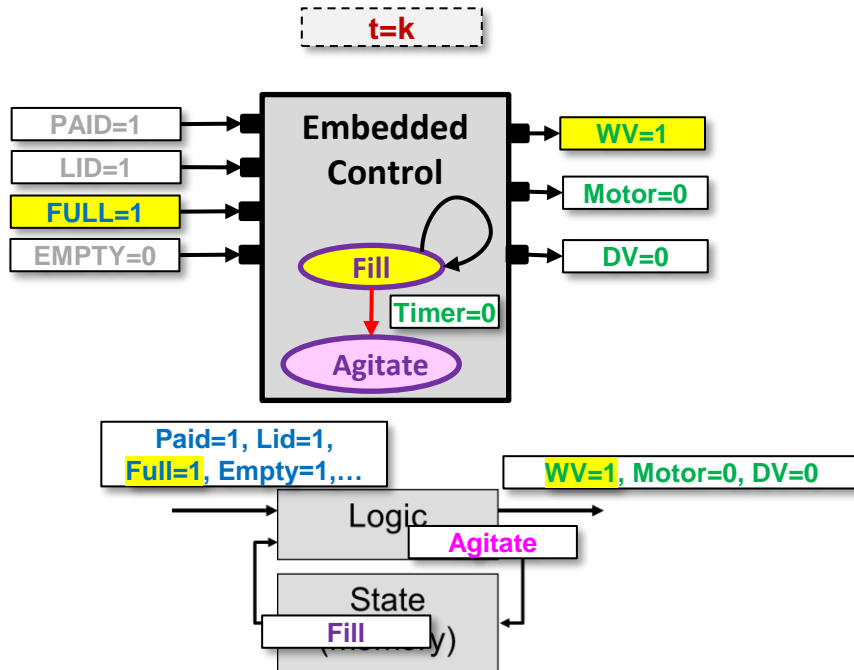
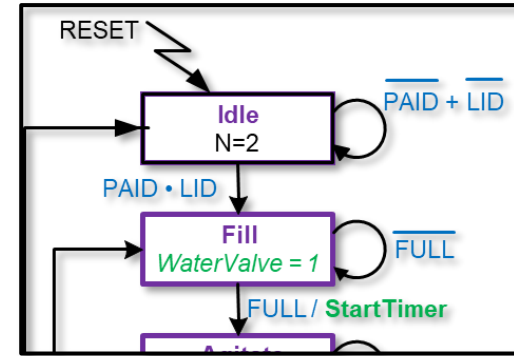
State Machine Operation (2)

- When the state changes, we produce new output values and may look at a new set of inputs



State Machine Operation (3)

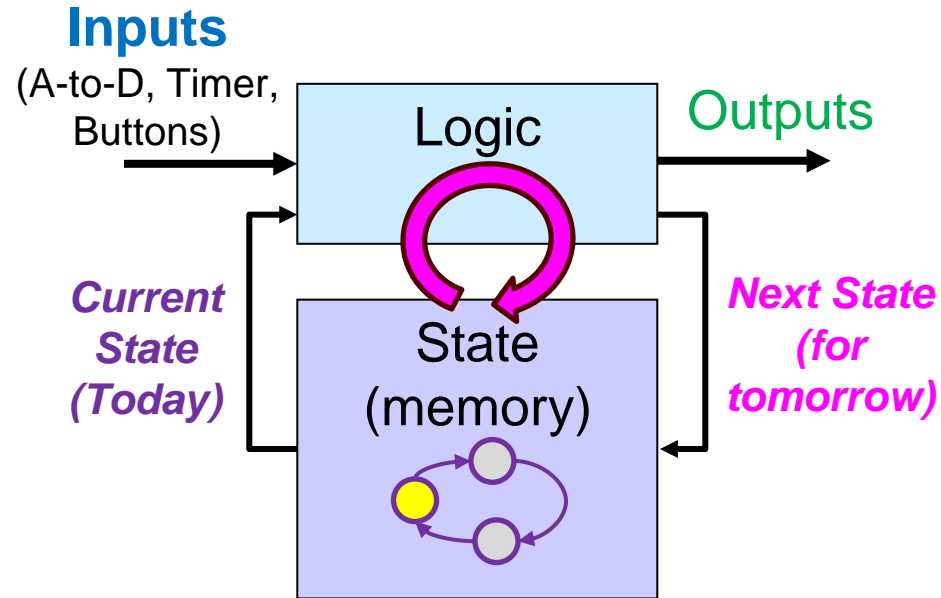
- We can use internal "time" inputs to control when we change states.



IMPLEMENTING STATE MACHINES IN SOFTWARE

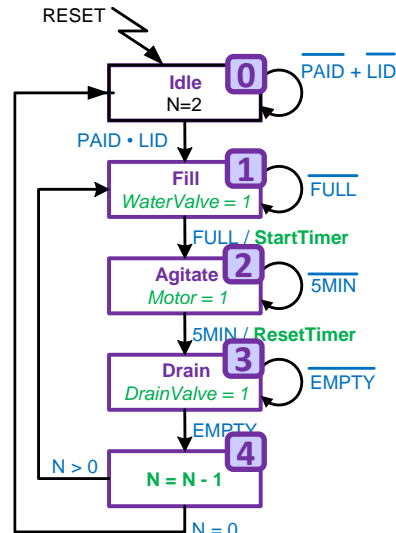
Software and Hardware Implementation

- Software Implementation
 - **Current State = just a variable(s)**
 - **Input/output** Logic = **if** statements to update the next state or produce outputs
 - `if(state == 0 && input == 1)`
`{ state = 1; output = 0; }`
 - Transitions triggered by input or timers
 - **We'll start by implementing state machines in SW**
- Later in the semester we'll see how to implement state machines in hardware



Coding State Machines 1

- Setup (declare and initialize) your state variable
 - Choose some numeric code for each state:
0=Idle, 1=Fill, 2 = Agitate, etc.
- Use **one while** loop and a single **delay** (or timer) to repeat the "day-in-the-life" routine of a state machine



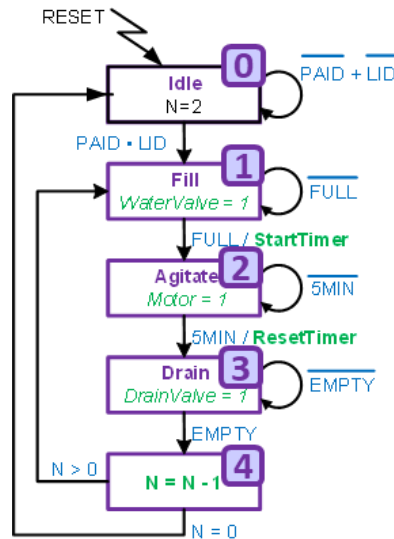
```

int main(){
    char currst = 0, n = 2; int timer;
    // other initialization
    while(1) {

        _delay_ms(100);
    }
    return 0;
}
  
```

Coding State Machines 2

- In the while loop, setup a series of **if..else if..else** statements to determine what **state** you are in "today"



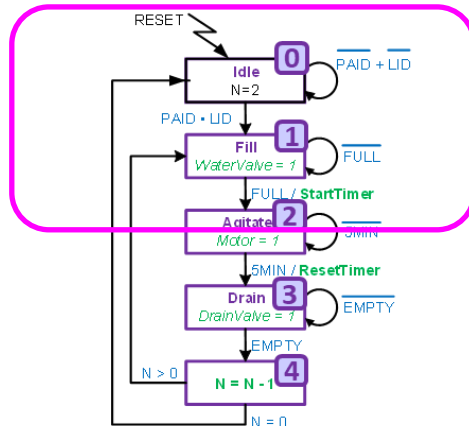
```

int main(){
    char currst = 0, n = 2; int timer;
    // other initialization
    while(1) {

        if( currst == 0 ){ // Idle
            // code pertinent to Idle
        }
        else if( currst == 1 ){ // Fill
            // code pertinent to Fill
        }
        else if( currst == 2 ){ // Agitate
            // code pertinent to Agitate
        }
        else if( currst == 3 ){ // Drain
            // code pertinent to Drain
        }
        else { // Decrement
            // code pertinent to last state
        }
        _delay_ms(100);
    }
    return 0;
}
  
```

Coding State Machines 3a

- Sample the inputs at the start of each iteration (each day)
- In each if statement for the current state, use a **nested** if statement for the **input conditions** to determine **next state** and **output** actions



```

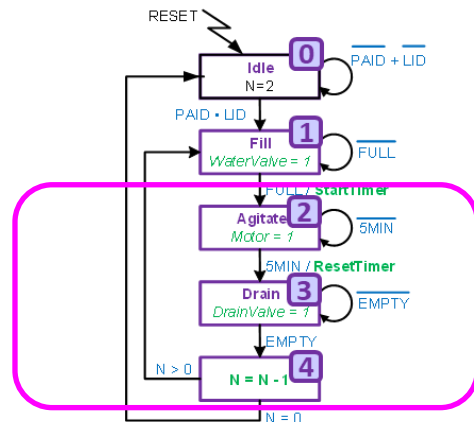
int main(){
  char currst = 0, n = 2; int timer;
  // other initialization
  while(1) {
    char paid = PIND & (1 << PD0);
    char lid = PIND & (1 << PD1);
    char full = PIND & (1 << PD2);
    if( currst == 0 ){ // Idle
      if(paid && lid)
        { currst = 1; /* Goto Fill */ }
    }
    else if( currst == 1 ){ // Fill
      PORTC |= (1 << PC0); // WV=1
      if(full)
        { currst = 2; timer = 0; }
    }
    else if( currst == 2 ){ // Agitate
      PORTC &= ~(1 << PC0); // WV=0
      PORTC |= (1 << PC1); // Motor=1
      ...
    }
    ...
    _delay_ms(100);
  }
  return 0;
}

```

Notice the nested IF statement structure used for state machines.

Coding State Machines 3b

- Sample the inputs at the start of each iteration (each day)
- In each if statement for the current state, use a **nested if statement** for the **input conditions** to determine **next state** and **output** actions



The final "else" is equivalent to "else if (currst == 4)".

```

int main(){
  char currst = 0, n = 2; int timer;
  while(1) {
    ...
    char full = PIND & (1 << PD2);
    char empty = PIND & (1 << PD3);
    ...
    else if( currst == 2 ){ // Agitate
      timer++;
      PORTC &= ~(1 << PC0); // WV=0
      PORTC |= (1 << 1); // Motor=1
      if(timer=3000) // 5 min
        { currst = 3; timer = 0; }
    }
    else if( currst == 3 ){ // Drain
      PORTC &= ~(1 << PC1); // Motor=0
      PORTC |= (1 << PC2); // DV = 1
      if(empty) { currst = 4; }
    }
    else { if(--n > 0) currst = 1;
           else currst = 0; }
      _delay_ms(100);
    }
  }
  return 0;
}

```

Notice the nested IF statement structure used for state machines.

Enumerations

- It would be nice to use **symbolic names** for states, rather than numbers
- In C/C++, **enumerations** associate an integer code (number) with a symbolic name
- Syntax:


```
enum [optional_collection_name] {SymName1, SymName2, ... SymNameN}
```

 - SymName1 = 0
 - SymName2 = 1
 - ...
 - SymNameN = N-1
- Use symbolic item names in your code and compiler will replace the symbolic names with corresponding integer values... **makes the code much more readable!**

```
const int IDLE=0;
const int FILL=1;
const int AGITATE=2;
...
char state = IDLE;
...
if(state == FILL && full == true) {
    state = AGITATE;
}
```

Option 1: Hard coding symbolic state names with given codes. Better than nothing, but enumerations (below) are often preferred.

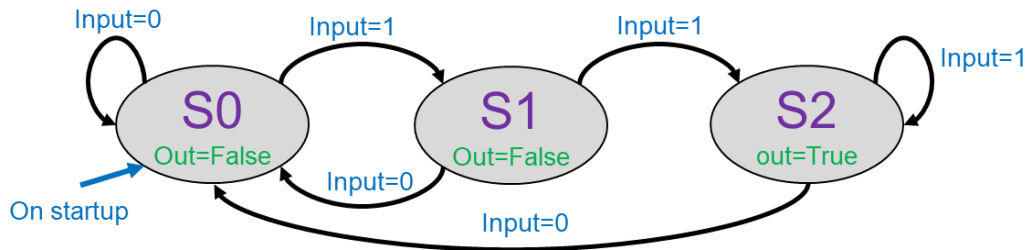
```
// First enum item is associated with code 0
enum States {IDLE, FILL, AGITATE, DRAIN, DEC};
// auto-assign 0      1      2      3      4
char state = IDLE;    // same as state = 0;
...
if(state == FILL && full == true) {
    state = AGITATE;    // same as state = 2;
}
```

Option 2: Using enumeration to simplify state coding and make the code **more readable!**

Another Example: 2 Consecutive 1's FSM

- How would we begin to code the implementation of this state machine?
 - Start with an **enum** to list the states
 - Declare and **initialize** your **state variable**
 - Choose or determine the **rate / delay** at which transitions in state should be made or output actions must occur.
 - 1 iteration of the loop handles 1 time step (a "day")

State Machine to check for two consecutive 1's on a digital input



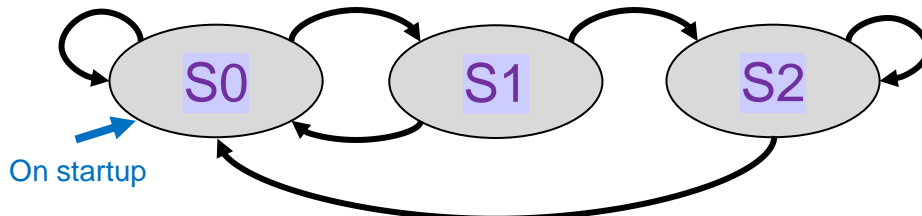
```

enum { S0, S1, S2 };
// input = PD0, output = PD7
int main()
{ // be sure to init. state
  unsigned char state=S0, input;
  while(1)
  {
    _delay_ms(10); // use approp. Time
  } return 0;
}
  
```


Consecutive 1's FSM – State

- Again, notice the structure:
 - The purple 'if' statements determine which state we are in

State Machine to check for two consecutive 1's on a digital input



```

enum { S0, S1, S2 };
// input = PD0, output = PD7
int main()
{ // be sure to init. state
  unsigned char state=S0, input;
  while(1)
  {
    if(state == S0){

    }
    else if(state == S1){

    }
    else { // state == S2

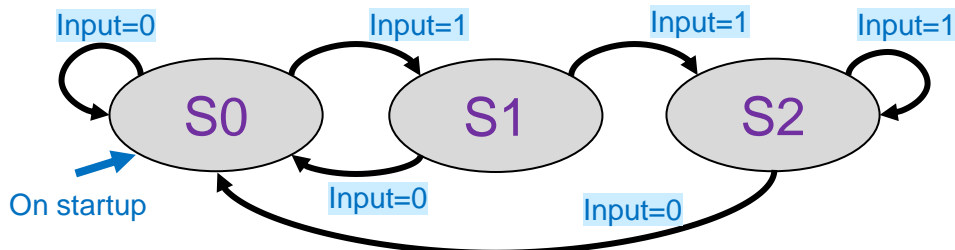
    }
    _delay_ms(10); // use approp. Time
  } return 0;
}
  
```

Select current state

Consecutive 1's FSM – Transitions

- Again, notice the structure:
 - The nested orange **'if'** statements determine which **input conditions** are true to determine how we **update the state**

State Machine to check for two consecutive 1's on a digital input



```

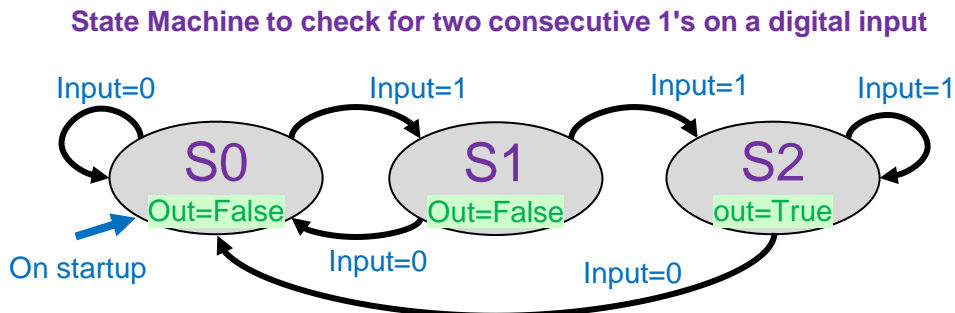
enum { S0, S1, S2 };
// input = PD0, output = PD7
int main()
{ // be sure to init. state
  unsigned char state=S0, input;
  while(1)
  {
    input = PIND & (1 << PD0);
    if(state == S0){
      if( input ){ state = S1; }
    }
    else if(state == S1){
      if( input ){ state = S2; }
      else { state = S0; }
    }
    else { // state == S2
      if( !input ) { state = S0; }
    }
    _delay_ms(10); // use approp. Time
  } return 0;
}
  
```

Select current state

Select input val.

Consecutive 1's FSM – Output Actions

- Again, notice the structure:
 - We can add appropriate **output** actions



```

enum { S0, S1, S2 };
// input = PD0, output = PD7
int main()
{ // be sure to init. state
  unsigned char state=S0, input;
  while(1)
  {
    input = PIND & (1 << PD0);
    if(state == S0){
      PORTD &= ~(1 << PD7);
      if( input ){ state = S1; }
    }
    else if(state == S1){
      PORTD &= ~(1 << PD7);
      if( input ){ state = S2; }
      else { state = S0; }
    }
    else { // state == S2
      PORTD |= (1 << PD7);
      if( !input ) { state = S0; }
    }
    _delay_ms(10); // use approp. Time
  } return 0;
}
  
```

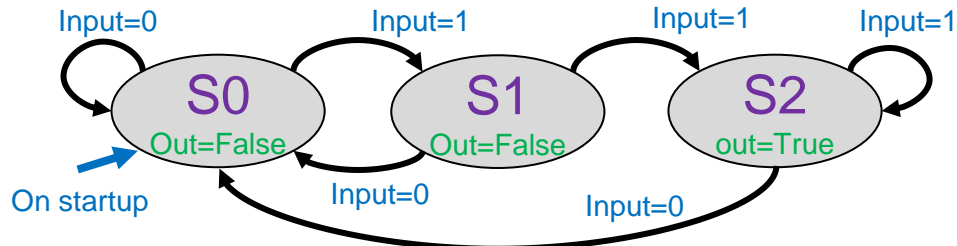
Select current state

Select input val.

Consecutive 1's FSM – Summary

- Again, notice the structure:
 - 1 iteration of the loop handles 1 time step (a "day")
 - The purple 'if' statements determine which state we are in and the nested orange 'if' statements determine which input conditions are true to determine how we update the state and what output actions we take
 - Some delay before the next iteration begins

State Machine to check for two consecutive 1's on a digital input



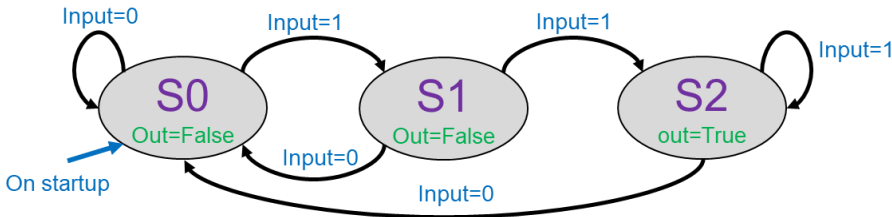
Select current state

```
enum { S0, S1, S2 };
// input = PD0, output = PD7
int main()
{ // be sure to init. state
  unsigned char state=S0, input;
  while(1)
  {
    input = PIND & (1 << PD0);
    if(state == S0){
      PORTD &= ~(1 << PD7);
      if( input ){ state = S1; }
    }
    else if(state == S1){
      PORTD &= ~(1 << PD7);
      if( input ){ state = S2; }
      else { state = S0; }
    }
    else { // state == S2
      PORTD |= (1 << PD7);
      if( !input ) { state = S0; }
    }
    _delay_ms(10); // use approp. Time
  }
  return 0;
}
```

A Potential Alternate Structure

- Sometimes, it may be easiest to **separate** :
 - the **state transition code** and
 - the **output action** code
- We can use separate **'if'** sequences.

State Machine to check for two consecutive 1's on a digital input



```

enum { S0, S1, S2 };
int main() {
  unsigned char state=S0, input;
  while(1) {
    // state transitions
    input = PIND & (1 << PD0);
    if(state == S0){
      if( input ){ state = S1; }
    }
    else if(state == S1){
      if( input ){ state = S2; }
      else { state = S0; }
    }
    else { // state == S2
      if( !input ) { state = S0; }
    }
  }
  // output actions
  if( state == S2)
    PORTD |= (1 << PD7);
  else
    PORTD &= ~(1 << PD7);
  _delay_ms(10); // use approp. Time
} return 0;
}
  
```

State transitions

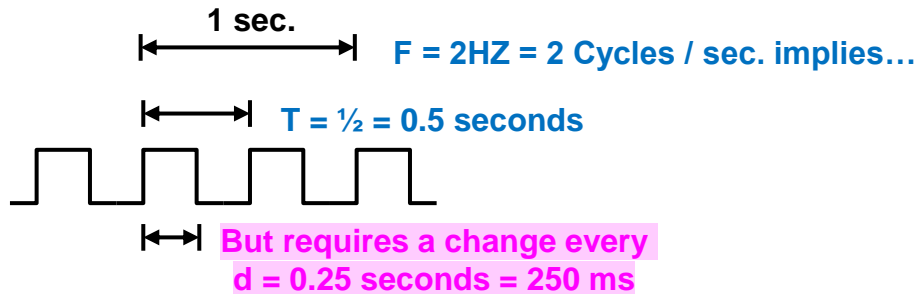
Outputs

State Machines as a Problem-Solving Technique

- Modeling a problem as a state machine is a powerful problem-solving tool
- When you need to write a program, design HW, or solve a more abstract problem at least consider if it can be modeled with a state machine
 - Ask questions like:
 - What do I need to remember to interpret my inputs or produce my outputs? [e.g. Checking for two consecutive 1's]
 - Is there a distinct sequence of "steps" or "modes" that are used (each step/mode is a state) [e.g. Washing machine, etc.]

A Note About Timing

- Write a program to blink an LED at **2HZ**
- What **delays** should you use?



- If all we are doing is blinking, we can simplify to use an **XOR** to flip the output bit

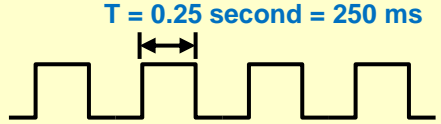
```
int main()
{
    // Initialization
    while(1)
    {
        PORTD |= (1 << 7); // LED on PD7
        _delay_ms(250);
        PORTD &= ~(1 << 7);
        _delay_ms(250);
    }
    return 0;
}
```

```
int main()
{
    // Initialization
    while(1)
    {
        PORTD ^= (1 << 7); // LED on PD7
        _delay_ms(250);
    }
    return 0;
}
```

Tunnel Vision (1)

- Consider a program that constantly monitors several inputs and takes appropriate actions:
 - If button1 is pressed it should blink an LED 10 times at a rate of 2 HZ
 - If button2 is pressed it should output something to the LCD screen
 - If button3 is pressed it should enable a motor
 - And even more tasks...
- To do something 10 times, it would be easiest to use a **for** loop, RIGHT?!?

```
// Ad-hoc implementation
int main()
{
  while(1)
  {
    int i;
    if(checkInput(1) == 0) {
      for(i=0; i < 10; i++) {
        blink(250); // on for 250, off for 250
                    // delays are in the blink() functions
      }
    }
    if(checkInput(2) == 0) {
      // output to LCD
    }
    if(checkInput(3) == 0) {
      // enable motor
    }
    if(...) {
      // even more tasks
    }
  }
  return 0;
}
```

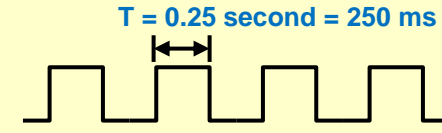


$T = 0.25 \text{ second} = 250 \text{ ms}$

Tunnel Vision (2)

- Consider a program that constantly monitors several inputs and takes appropriate actions:
 - If button1 is pressed it should blink an LED 10 times at a rate of 2 HZ
 - If button2 is pressed it should output something to the LCD screen
 - If button3 is pressed it should enable a motor
 - And even more tasks...
- To do something 10 times, it would be easiest to use a **for** loop, RIGHT?!?
- No! When we are in the **for** loop, we would not be performing our other tasks and miss actions.

```
// Ad-hoc implementation
int main()
{
  while(1)
  {
    int i;
    if(checkInput(1) == 0) {
      for(i=0; i < 10; i++) {
        blink(250); // on for 250, off for 250
        // what if button 2, 3, ... are pressed?
      }
    }
    if(checkInput(2) == 0) {
      // output to LCD
    }
    if(checkInput(3) == 0) {
      // enable motor
    }
    if(...) {
      // even more tasks
    }
  }
  return 0;
}
```



A Better Approach



To keep many things going at once, cycle through all the tasks doing only a short / small amount of the task at a time!

A Better Approach

- Instead, perform 1 blink **per** iteration, tracking your count!
- This allows other checks and actions to be performed after each single blink
- You can use your count as a "state" variable:
 - cnt: 0-9 tracks how many blinks
 - cnt: 10 DONE/OFF
- ...or use a separate state variable (**s=1**: counting, **s=0**: DONE/OFF) in combination with **cnt**
- Every time we press button 1, we reset the cnt to start 10 more blinks

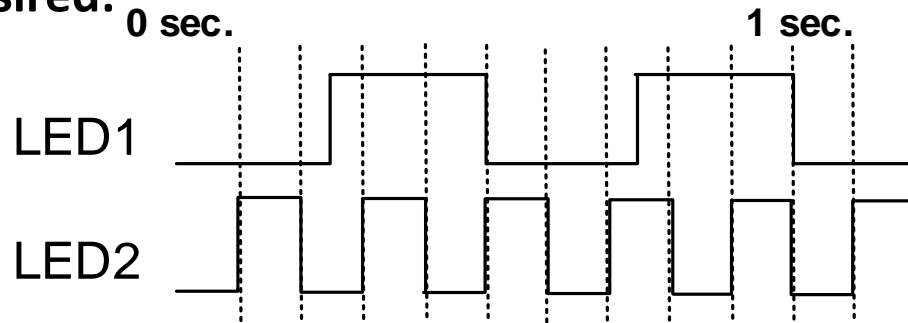
Other checks and actions

```
// Ad-hoc implementation
int main()
{
    int cnt=10;
    while(1)
    {
        if(checkInput(1) == 0) {
            cnt=0;
        }
        if(cnt < 10) {
            blink(250); // 1 blink per iter.
            cnt++;
        }
        if(checkInput(2) == 0) {
            // output to LCD
        }
        if(checkInput(3) == 0) {
            // enable motor
        }
        if(...) {
            // more tasks
        }
    }
    return 0;
}
```

Operations at Different Rates (1)

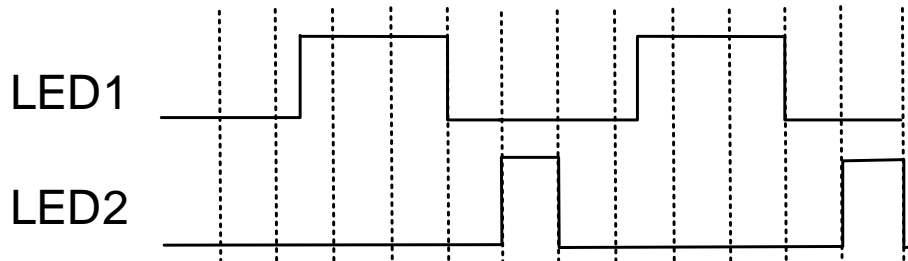
- Consider a program to blink one LED at a rate of 2 Hz and another at 5 Hz at the same time

- Desired:**



- Problem:** Does the code to the right work correctly?

- No! When one LED blinks the other will be off



```
int main()
{
    while(1)
    {
        LED1_OFF();
        _delay_ms(250);
        LED1_ON();
        _delay_ms(250);

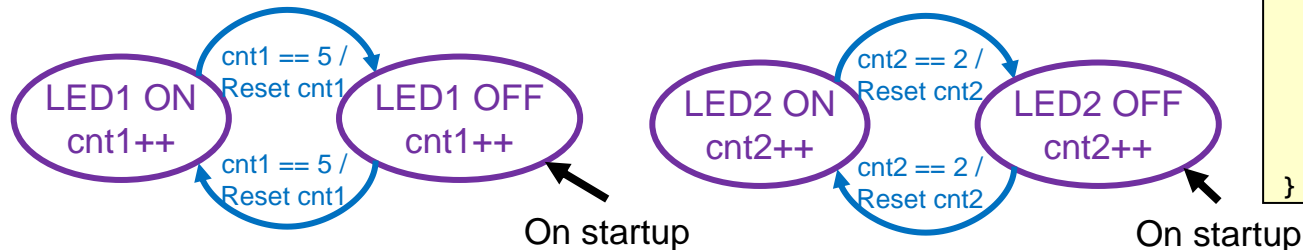
        LED2_OFF();
        _delay_ms(100);
        LED2_ON();
        _delay_ms(100);

    }

    return 0;
}
```

Operations at Different Rates (2)

- Use a SINGLE delay and separate state (**count**) variables to do work on each task at the "same time". This mimics "parallel" (aka multithreaded) execution.
- To determine that delay, find the **GCD (Greatest Common Divisor)** of the **minimum periods** that action is needed for each task.
 - **Task 1:** Flip the LED every **250 ms**
 - **Task 2:** Flip the LED every **100 ms**
 - Use a delay of **50ms = GCD (250, 100)**



```
int main()
{
    int cnt1 = 0, cnt2 = 0;

    // set initial state of LEDs as "off"
    LED1_OFF();
    LED2_OFF();

    while(1)
    {
        if(cnt1 == 5)
        {
            FLIP_LED1();
            cnt1 = 0;
        }
        cnt1++;
        if(cnt2 == 2)
        {
            FLIP_LED2();
            cnt2 = 0;
        }
        cnt2++;
        // Delay the minimum granularity
        _delay_ms(50);
    }
    return 0;
}
```

Operations at Different Rates (3)

- To determine that delay, find the **GCD (Greatest Common Divisor)** of the **minimum periods** that action is needed for each task.
 - **Task 1:** Flip the LED every **250 ms**;
 - **Task 2:** Flip the LED every **100 ms**
 - Use a delay of **50ms = GCD (250, 100)**
- We can use a single counter looking for multiples of the individual task periods (every 2 or every 5 iterations) using the modulo operator
- Can **reset the count to 0** after the **Least Common Multiple** of the task periods
 - **LCM(250,100) = 500ms = 10 iterations.**

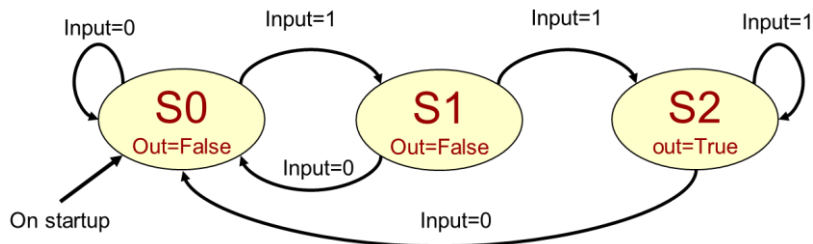
```
int main()
{
    int cnt = 0;

    // set initial state of LEDs as "on"
    LED1_ON();
    LED2_ON();

    while(1) {
        if(cnt % 5 == 0) {
            FLIP_LED1();
        }
        if(cnt % 2 == 0) {
            FLIP_LED2();
        }
        cnt++;
        if(cnt == 10)
            { cnt = 0; }
        // Delay the minimum granularity
        _delay_ms(50);
    }
    return 0;
}
```

Summary Definition

- To specify a state machine, we must specify 6 things:
 - A set of possible input values: $\{0, 1\}$
 - A set of possible states: $\{S0, S1, S2\}$
 - A set of possible outputs: $\{\text{False}, \text{True}\}$
 - An initial state = S0
 - A transition function:
 - $\{\text{States} \times \text{Inputs}\} \rightarrow \text{the Next state}$
 - An output function:
 - $\{\text{States} \times \text{Inputs}\} \rightarrow \text{Output value(s)}$



All the info in the state diagram is presented in the sets and tables to the right

Inputs: $\{0, 1\}$

States: $\{S0, S1, S2\}$

Outputs: $\{\text{False}, \text{True}\}$

Initial State: S0

	Inputs	
State	0	1
S0	S0	S1
S1	S0	S2
S2	S0	S2

State Transition Function

State	Outputs
S0	False
S1	False
S2	True

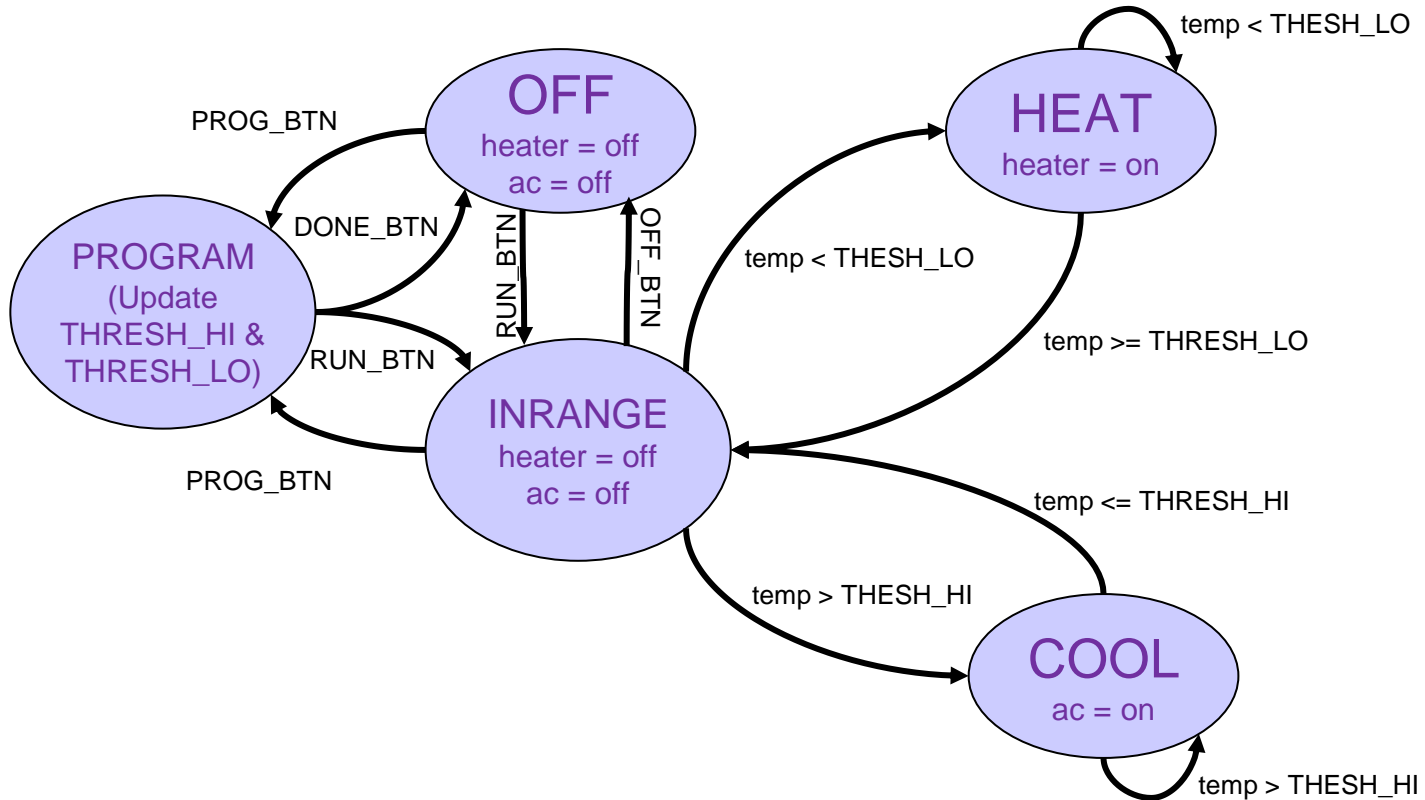
Output Function

HW (Instruction Cycle) & Software (String Matching)

MORE EXAMPLES IF TIME

Thermostat

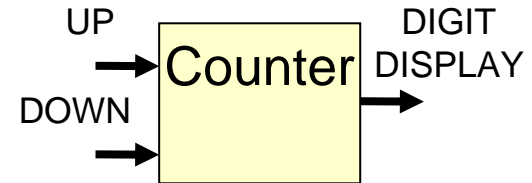
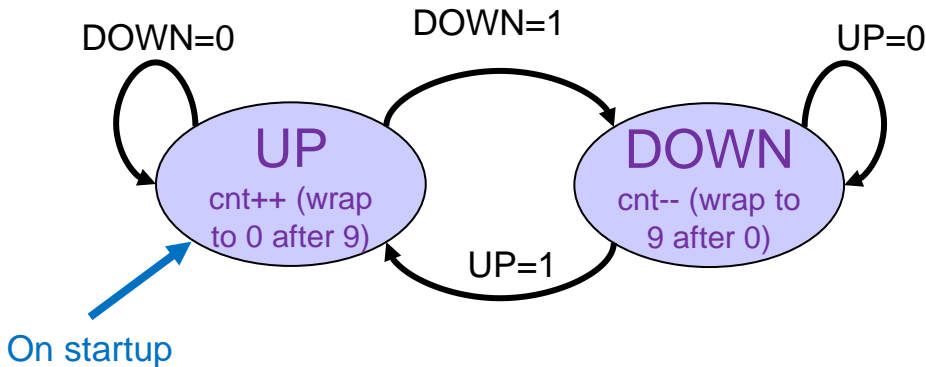
- Sample state machine to control a thermostat



Counter Example

- Consider a system that has two button inputs: UP and DOWN and a 1-decimal digit display. It should count up or down at a rate of 500 milliseconds and change directions only when the appropriate direction button is pressed
- Every time interval we need to poll the inputs to check for a direction change, update the state and then based on the current state, increment or decrement the count

State Machine to count up or down (and continue counting) based on 2 pushbutton inputs: UP and DOWN



More State Machines

- State machines are all over the place in digital systems
- Instruction Cycle of a computer processor

