Spatial Relations Defined

This topic summarizes how spatial predicates are defined:

- » Background
- » Boundary, Interior, and Exterior
- » String Representations of Intersection Matrices
- » Definitions of Predicate Attributes

For definitive documentation on spatial relations, please consult the OGC documentation on spatial relations.

Click here to see an example that illustrates different <u>spatial relationships</u>.

Spatial Predicates

Background

The definitions of each Predicate attribute are given in the tables included under this heading. This section also gives specific definitions of boundaries, exteriors, and interiors as they apply to specific feature types and explains the concept of an intersection matrix.

Each feature – whether it's a point, line, or polygon – has a definition of an INTERIOR, BOUNDARY, and EXTERIOR. The EXTERIOR is everything that is not on the BOUNDARY or the INTERIOR.

Spatial relations are undefined for geometries that are not OGC valid or aggregate geometries.

Boundary, Interior, and Exterior

BOUNDARY	Points	Empty set.	
	Lines	CURVE_BOUNDARY_RULE ENDPOINTS_MOD2	
		The boundary is the set of all endpoints that occur an odd number of times. For a simple linear feature (that is, not a multicurve), this means the boundary is comprised of the start and end points, unless the line is closed (the start and end are the same point), in which case the boundary is the empty set. (This is the default if CURVE_BOUNDARY_RULE is unspecified.) CURVE_BOUNDARY_RULE ENDPOINTS_ALL The boundary is the set of all and points_regardless of the	
		endpoints, regardless of the number of times they occur in the geometry.	
	Polygons	The border of a polygon, including the border of the holes.	
INTERIOR	Points	The point location.	
	Lines	The entire line except its boundary as determined above.	
	Polygons	The inner surface of the polygon.	

Dimensionally Extended 9 Intersection Matrix

The comparison of two features produces a 3 x 3 matrix known as the Dimensionally Extended 9 Intersection Matrix (DE-9IM), shown below:

		candidate			
		interior	boundary	exterior	
base	interior	c ₀	c ₁	c ₂	
	boundary	c ₃	c ₄	c ₅	
	exterior	c ₆	c7	c ₈	

The value of each element of the matrix indicates the dimension of the geometry produced by intersecting the given parts of the two features. The dimension is one of the following:

- -1 there is no interaction
- 0 the intersection produces a point
- 1 the intersection produces a line
- 2 the intersection produces a surface

So for instance, if c_1 is 1, then the intersection of the base's interior with the candidate's boundary produces a line. This could occur when both features are polygons and they overlap.

Each of the predicates can be defined in terms of what the intersection matrix of the two features must look like. For this, use a pattern matrix. Each

element of the pattern matrix can be one of the following:

- \ast the value of this element may be anything (-1, 0, 1, or 2)
- T the value of this element must be 0, 1, or 2
- F the value of this element must be -1
- 0 the value of this element must be 0
- 1 the value of this element must be 1
- 2 the value of this element must be 2

The pattern matrix for the *disjoint* predicate is:

F	F	*
F	F	*
*	*	*

This means that neither feature's interior or boundary may interact with the other's interior or boundary.

String Representations of Intersection Matrices

Any intersection matrix can be represented as a 9-character string. To generate the string representation of a particular intersection matrix, take each element starting from the top-left, going right-to-left for each row.

For example, the string representation of the intersection matrix for the *disjoint* predicate (as seen above) is "FF*FF****".

Definitions of Predicate Attributes

Each of the supported predicates is described below, along with some associated examples and pattern matrices. Note that the examples are not exhaustive: there may be entirely different situations where a given predicate is true. In the examples, the base is labeled "A" and the candidate is labeled "B".

Example	Description	Pattern Matrix
	The two features are not disjoint, as defined below.	
(A) (B)	The boundaries and interiors do not intersect.	F F '
(B)	The features have the same boundary and the same interior.	T * F
AB A B	The boundaries may intersect or one boundary may intersect the other interior.	F T *
	The interiors do not touch.	or
	Undefined for point/point.	F
		or
		F * * * * * * * * * * * * * * * * * * *
Å B	The interiors intersect and the base's interior intersects the candidate's exterior. Or in the case of line/line, the intersection of the interiors forms	T * T
	a point.	or, for two lines:
	Undefined for point/point or area/area. Undefined for aggregate/multi geometries.	0 ^ ^
௸	The interiors intersect, but neither feature is contained by the other, nor are the features equal.	T * T
	Undefined for point/line, point/area,	or, for two lines:
	or line/area. Undefined for aggregate/multi geometries.	1 ^ T
A B	The interiors intersect and no part of the candidate's interior or boundary intersects the base's exterior. It is possible for the boundaries to	T
	A B A B	The two features are not disjoint, as defined below. The boundaries and interiors do not intersect. The features have the same boundary and the same interior. The boundaries may intersect or one boundary may intersect the other interior. The interiors do not touch. Undefined for point/point. The interiors intersect and the base's interior intersects the candidate's exterior. Or in the case of line/line, the intersection of the interiors forms a point. Undefined for point/point or area/area. Undefined for aggregate/multi geometries. The interiors intersect, but neither feature is contained by the other, nor are the features equal. Undefined for aggregate/multi geometries. The interiors intersect and no part of the candidate's interior or boundary intersects the base's exterior. It is

Predicate	Example	Description	Pattern Matrix	
		intersect.		
		(inverse of WITHIN)		
WITHIN		The interiors intersect and no part of the base's interior or boundary intersects the candidate's exterior. It is possible for the boundaries to intersect. (inverse of CONTAINS)	T	

Undefined for aggregate/multi geometries.

Spatial Relationship Examples

Spatial Relationship Examples						
			Candidates			
elations	Base	•				
Contains	•	•	×	×		
				×		
		•				
Crosses	•	×	×	×		
		×	X			
		×		×		
	•	•	×	×		
		×	/	×		
	Contains	Contains Crosses	Contains Crosses	elations Base Contains Contains Crosses Crosses		

			×	×	
		•	×	×	×
	Overlaps	/	×	/	×
			×	×	
		•	×	/	
	Touches	/		\overline{Z}	> □
		•	•	/	·
	Within		×	/	
			×	×	
Disjo		•	• •	·/	•
	oint	/	/	//	