

## ANSWER KEY: Heap Coding Practice for Midterm (CSCI 104 Spring 2024)

You have a 5-ary Pokémon MinHeap that uses a vector container of `std::pair` based on 0-indexing. The `std::pair` has a `.first` of rarity (double) and a `.second` of name (`std::string`). The heap property is based on the rarity of a Pokémon. Assume that you have working implementations of `trickleUp()` and `trickleDown()` if you need it.

Here's the class you will be using (incomplete but it's enough to do the problem):

```
class Pokemon_MinHeap {
public:
    void updateRarity(std::string target_name, double new_rarity);
    void defeat();
    void multi_defeat(int x);

private:
    std::vector< std::pair<double, std::string> > pokemons;
    void trickleDown(int x);
    void trickleUp(int x);
};
```

### PROBLEM 1.1:

A Pokémon was found to be more common than originally anticipated. We want to update our data structure to reflect that. You can assume that the value of `new_rarity` will always be greater than the Pokémon's current rarity. To do this, implement:

```
void Pokemon_MinHeap::updateRarity(std::string target_name, double new_rarity)
```

More specifically, you should:

1. Search the MinHeap for a Pokémon name that matches the `target_name` parameter. If a matching name cannot be found, throw `std::invalid_argument()`.

2. If a matching name is found, update the correct Pokémon's rarity and make sure you maintain the heap property (remember that rarity can only increase in this problem).

Solution Code:

```
void Pokemon_MinHeap::updateRarity(std::string target_name, double new_rarity)
{
    for(unsigned int i = 0; i < pokemons.size(); i++){
        if(pokemons[i].second == target_name){ // if found
            pokemons[i].first = new_rarity;
            trickleDown(i); // maintain heap property
            return; // done
        }
    }
    throw std::invalid_argument(); // if not found
    return; // never reached but gets rid of warnings
}
```

### PROBLEM 1.2:

What is the runtime complexity of `Pokemon_MinHeap::updateRarity()`? Justify your answer.

Answer:  $O(n)$  due to the for-loop.

Note: Big-theta is also acceptable.

Note: `trickleDown()` is only operated once, making  $n + \log n \rightarrow O(n)$ .

### PROBLEM 2.1:

We want to hunt down the rarest Pokémon possible.

Implement `void Pokemon_MinHeap::defeat()` to defeat the rarest Pokémon.

More specifically, you should:

1. Throw an `std::underflow_error()` if there is nothing to remove.
2. If there is something to remove, remove the rarest Pokémon (the Pokémon with the lowest rarity value) while maintaining the heap property.

Solution Code:

```
void Pokemon_MinHeap::defeat()
{
    if( pokemons.size() <= 0 ){
        throw std::underflow_error();
    }
    else {
        pokemons[0] = pokemons[pokemons.size() - 1];
        pokemons.pop_back();
        trickleDown(0);
    }

    // Runtime is O(log n) due to trickleDown(). Big-theta notation is also valid
}
```

### PROBLEM 2.2:

What is the runtime complexity of `Pokemon_MinHeap::defeat()` ?

Answer:  $O(\log n)$ .

Note: Big-theta is also acceptable.

Note: Runtime comes from the `trickleDown()` algorithm runtime.

### PROBLEM 3.1:

Now that you have a hopefully working defeat implementation, we now want to defeat the  $x$  rarest Pokémon based on user inputs. To do this, implement

```
void Pokemon_MinHeap::multi_defeat(int x).
```

More specifically, you should:

1. Check if there are enough Pokémon to defeat based on  $x$  and check if  $x$  is at least 1. If either check fails, throw `std::underflow_error()`.

2. If the checks are successful, defeat  $x$  amount of Pokémon by updating the MinHeap and maintaining the heap property. You are also allowed to use your coded implementations from previous problems (assume they work properly).

Solution Code:

```
void Pokemon_MinHeap::multi_defeat(int x)
{
    if( pokemons.size() < x || x <= 0 ){
        throw std::underflow_error();
    }
    else {
        for(int i = 0; i < x; i++){
            defeat();
        }
    }
}
```

### PROBLEM 3.2:

What is the runtime complexity of `Pokemon_MinHeap::multi_defeat()` ? Use Big-O notation.

Answer:  $O(n \log n)$ .

Note:  $O(n)$  due to the for-loop and each iteration is executing a  $O(\log n)$  algorithm.

Long Answer (you don't need to know this, but this is more correct due to the size of the array changing after each call to defeat):

- Overall, we get a pattern like  $O((\log n) + (\log n-1) + \dots + (\log 2) + (\log 1))$ .
- $O(\sum_{i=1}^n \log(i))$  would also work.
- By properties of log:  $\log(1) + \log(2) + \dots + \log(n) = \log(1 * 2 * \dots * n) = \log(n!)$
- So we now have  $O(\log(n!))$ .
- $O(n!)$  is asymptotically less than  $O(n^n)$ . As for why, please see this [proof](#).

-  $O(\log(n!)) = O(\log(n^n)) = O(n \log(n))$ .

**PROBLEM 4.1 (unrelated to previous problems):**

When is `trickleUp()` normally used?

Answer: To maintain the heap property after inserting a new element.