Lab 8: BST (and AVL)

CSCI104

REMEMBER: Heaps

- COMPLETE d-ary tree
 - All levels except the last are completely filled
 - All leaves in last level are to the left side
- Every parent is "better" than both of its children
- Min Heap: node is less than or equal to all children
- Max Heap: node is greater than or equal to all children





Could this be a heap??

Binary Search Trees (BST)

- Not necessarily a complete or full tree
- Left children (left subtree) hold values LESS THAN or equal to parent's values
- Right children (right subtree) hold values GREATER THAN parent's value







Traversals: Pre-Order, In-Order, Post-Order

- All traverals operate on EVERY node eventually-just in different orders
 - "Pre" : visit the parent "pre-" (before) visiting left and right sub-trees.
 - "In" : visit the parent "in"-between visiting left and right sub-trees.
 - "Post": visit the parent "post-" (after) visiting left and right sub-trees.

Pre-Order Traversal

- // Operate on current node
- // Recurse left
- // Recurse right
- // return

In-Order Traversal

- // Recurse left
- // Operate on current node
- // Recurse right
- // return

Post-Order Traversal

- // Recurse left
- // Recurse right
- // Operate on current node
- // return

Traversals in C++

For a BST, what is special about operating on elements using an in-order traversal? If we were printing integers using this traversal, what would the output look like? void pre_order(Node* node) {
 if (node == nullptr) return;
 print(node);
 pre_order(node->left);
 pre_order(node->right);

}

void in_order(Node* node) {
 if (node == nullptr) return;
 in_order(node->left);
 print(node);
 in_order(node->right);
}

void post_order(Node* node) {
 if (node == nullptr) return;
 post_order(node->left);
 post_order(node->right);
 print(node);

Why BSTs? SEARCHING!

- Enable (potentially) faster searching
- Why do we say potentially? What is an example where the search is slow, even if it's a valid BST?

Why BSTs? SEARCHING!



Slower search: O(n) Basically like a linked list Faster search: O(logn)

Search Function

• Can do it iteratively or recursively

To search for key \mathbf{x} in a BST, we compare X to the current node.

- If the current node is null, X must not reside in the tree.
- If **x** is equal to the current node, simply return the current node.
- If it is less than the current node, we check the left subtree.
- Else, it must be greater than the current node, so we check the right subtree.

Or, in code:

```
// Finds the node with value == val inside the bst. Returns nullptr if not found
Node* find(Node* root, int val) {
    if (root == nullptr) return nullptr;
    if (root->val == val) return root;
    if (root->val > val) return find(root->left, val);
    return find(root->right, val);
}
```

Recursive example

Search Example



Operation: find(6) // We begin at the root Let's walk through this:

- Current node = 8, 6 < 8, therefore go left.
- Current node = 3, 6 > 3, therefore go right.
- Current node = 6, 6 = 6, we've found the node.

Operation: find(0) // We begin at the root Let's walk through this one too:

- Current node = 8, 0 < 8, therefore go left.
- Current node = 3, 0 < 3, therefore go left.
- Current node = 1, 0 < 1, therefore go left.
- Current node = null. 0 is not in the tree.

Balanced Binary Tree

- Height-balancing property: heights of each subtree differ by no more than 1
- Avoids the slower search times!
- Keeps the height of the tree log(n)



A is balance, B is not

Maintaining BST Property

- REMEMBER: BST Property = left subtree node keys less than parent's and right subtree node keys greater than parent's
- Maintained by **smart** insertion and deletion
- Insert function
 - Traverse the tree based on key to be inserted
 - Insert once you encounter a situation where you cannot traverse further
- Remove function
 - Need to choose which node to promote
 - If node you want to remove has 0 children: just remove it
 - If node you want to remove has 1 child: promote the child of the node
 - If node you want to remove has 2 children: swap with its predecessor OR successor

Self-Balancing BSTs

- We will be focusing on AVL trees
- You keep the tree balanced even after insertions or deletions
- This involves using rotations!

Single Rotations RIGHT





Single Rotations LEFT





Double Rotations RIGHT LEFT





Double Rotations LEFT RIGHT





Left rotate on y, then right rotate on z



AVL Insert and Remove

• Insert

- Insert as you would in a BST
- Fix the tree if it is unbalanced after inserting the node (ROTATION)
 - Need at most 1 rotation (either a single or double rotation)

• Remove

- \circ $\,$ Remove as you would in a BST $\,$
- Keep traversing up the tree and fixing tree if unbalanced (ROTATIONS)
 - You may need multiple rotations to fully fix the tree

The Lab

- Implement the rangeSum function, isBalanced function (will be helpful for your PA!), and levelOrder function
- Use <u>make</u> to run all tests; show a TA/CP

