Recall our formulas:

- **Arithmetic Series:**
  \[ \sum_{i=0}^{n} \Theta(i^p) = \Theta(n^{p+1}) \]

- **Geometric Series:**
  \[ \sum_{i=0}^{n} c^i = \Theta(c^n) \]

- **Harmonic Series:**
  \[ \sum_{i=1}^{n} \frac{1}{i} = \Theta(\log n) \]
Let’s determine the runtime of this algorithm:

**Algorithm 1 Number Filtering**

1: **Input:** a positive integer \( n \geq 2 \)
2: initialize the Boolean array \( nums \) such that \( nums(i) = True \) for \( i = 2, \ldots, n \)
3: for \( i = 2, \ldots, n \) do
4:     for \( j = 2, \ldots, \left\lfloor \frac{n}{i} \right\rfloor \) do
5:         if \( i \times j \leq n \) then
6:             \( nums(i \times j) = False \)
7:         end if
8:     end for
9: end for
Recursion

Given the heads of two sorted linked lists, return the merged, sorted linked list.

Adapted from merge sort.
## ADTs

<table>
<thead>
<tr>
<th>Type</th>
<th>Key Points</th>
<th>Operation Runtimes</th>
<th>Examples</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>List</strong></td>
<td>Ordered, access based on position (index), may contain duplicates</td>
<td>Depends on implementation</td>
<td>A music album, a book series</td>
</tr>
<tr>
<td><strong>Stack</strong></td>
<td>LIFO (last in first out)</td>
<td>Push, pop, top</td>
<td>A stack of trays at a cafeteria, tandem parking lot, “undo”</td>
</tr>
<tr>
<td><strong>Queue</strong></td>
<td>FIFO (first in first out)</td>
<td>Push back, pop front, front</td>
<td>Waiting in line for a cashier at a store, printing a document</td>
</tr>
<tr>
<td><strong>Map</strong></td>
<td>Stores key, value pairs, keys must be unique (but values can have duplicates), no inherent ordering</td>
<td>Insert, remove, find/lookup: All O(log n)</td>
<td>A dictionary, a grade book (key: student, value: grade)</td>
</tr>
<tr>
<td><strong>Set</strong></td>
<td>Like a map but only store keys, items must be unique, accessed based on keys, not indices</td>
<td>Insert, remove, find/lookup: All O(log n)</td>
<td>Spices in a cupboard, all USC courses</td>
</tr>
<tr>
<td><strong>Priority Queue</strong></td>
<td>Self-orders items based on value, only allows retrieval/removal of the &quot;best&quot; priority item</td>
<td>Push, pop, top O(log n), O(log n), O(1)</td>
<td>A hospital where patients arrive with injuries of varying severity</td>
</tr>
</tbody>
</table>
**ADTs**

1. In operating systems, multiple processes can happen concurrently with the use of threads. What ADT could you use to store processes, where they are assigned to threads based on the order in which they were first requested?
   a. What if processes were now instead handled by their level of importance?
2. Say you’re a teacher and you want to keep track of your students and their emergency contacts. What data structure should you use?
3. Say you want to keep track of every single line of code you write in a C++ class. What data structure should you use?
4. Say you’re trying to write a simple Towers of Hanoi implementation. What data structure should you use for each peg?

*In Towers of Hanoi, you can only remove the top ring*
Stacks & Queues

Given this directed graph, use a stack and a queue to find a path from node 0 to node 3. Show the current state of the stack and queue in each iteration of the search and break ties from the node’s value, pushing higher numbered neighbors on first. Do not revisit nodes!
Heaps

**Review:** Store a heap in an array

Array starting at index 0, given location i:

- **Parent Location:** \((i - 1) / 2\)
- **Left Child:** \(2i + 1\)
- **Right Child:** \(2i + 2\)
Pushing + Popping a Heap

Push:

1. Insert to next index (bottom of tree)
2. Swap with parent until it’s not “better than” its parent, or is now the root

Pop:

1. Swap 0th element (thing to be popped) with last element, delete
2. Swap root element down til in correct spot
Heap Example

Given the array: [1, 5, 2, 25, 15, 10, 20, 50, 60, 3]

What does it look like as a binary heap in tree form? Is it a valid heap? If it is, what type of heap? If it isn’t, what swap(s) do we need to make to make it valid?
Inheritance

Explain the difference between public, protected, and private inheritance.

How does the visibility of inheritance affect:

- Public member variables?
- Protected member variables?
- Private member variables?
Inheritance Example

- What can Island access?
- What can Atoll access?
Inheritance Example

Island is now a PRIVATE GeographicFeature.

- What can Island access?
- What can Atoll access?