## DO NOT OPEN EXAM PACKET UNTIL INSTRUCTED TO DO SO

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## PLEASE TURN OFF ALL ELECTRONIC DEVICES

| ID\#: |  |
| :--- | :--- |
| Name: |  |

- This exam is closed book. You are allowed one (1) 8.5 " $\times 11$ " handwritten note sheet
- You will have eighty (80) minutes to complete this exam.
- Answer the questions only in the spaces provided on the question sheets.
- If you give multiple solutions to a problem without indicating which one you want graded, the grader may select one to grade.
- Your answers do not need to be complete, grammatically correct sentences.

| Problem | Points | Possible |
| :--- | :--- | :--- |
| 1 |  | 8 |
| 2 |  | 4 |
| 3 |  | 4 |
| 4 |  | 6 |
| 5 |  | 4 |
| 6 |  | 7 |
| 7 |  | 47 |
| 8 |  | 7 |
| Total |  |  |

1. Solve the following project one style problem.
```
/*
    * isAsciiDigit - return 1 if 0x30 <= x <= 0x39 (ASCII codes for characters '0' to '9')
    * Example: isAsciiDigit(0x35) = 1.
    * isAsciiDigit(0x3a) = 0.
    * isAsciiDigit(0x05) = 0.
    * Legal ops: ! - &^ | + << >>
    * Max ops: }1
    */
int isAsciiDigit(int x) {
    int neg_0x30 = ~(0x30) + 1;
    int x_minus_0x30 = x + neg_0x30;
    int neg_0x3a = ~(0x3a) + 1;
    int x_minus_0x3a = x + neg_0x3a;
    int lower_bound_mask = !(x_minus_0x30 >> 31); //0 if x >= 0x30, 1 if x < 0x30
    int upper_bound_mask = !!(x_minus_0x3a >> 31); //0 if x > 0x3a, 1 if x <= 0x39
    return lower_bound_mask & upper_bound_mask; //TOTAL OPS: }1
}
```

2. Write the following base-10 integers in eight-bit two's complement. Express your answer in both binary and hex (base-16).
a. 53

$$
\begin{aligned}
& 53=32+16+4+1 \\
& 53=00110101 \\
& 0011->3 \quad 0101->5 \quad 53=0 \times 35
\end{aligned}
$$

b. -75

$$
\begin{aligned}
& -75=-128+32+16+4+1 \\
& -75=10110101 \\
& 1011->11-->b \quad 0101->5 \quad-75=0 x b 5
\end{aligned}
$$

3. Interpret the following as hex representations of two's complement integers (eight bits each). Write them both in binary and in base-10.
a. $0 x C F$

$$
\begin{array}{lrl}
c \rightarrow 12 \rightarrow 1100 \quad f \rightarrow 15 \rightarrow 1111 & 0 x C F=11001111 \\
0 x C F=-128+64+8+4+2+1=-49 &
\end{array}
$$

b. $0 \times 49$

$$
4 \rightarrow 0100 \quad 9 \rightarrow 1001 \quad 0 \times 49=01001001
$$

$$
0 \times 49=64+8+1=73
$$

4. Consider the eight-bit floating point format. In eight-bit floating point, there is one sign bit, three exponent bits, and four fractional bits. The exponent bias is 3 .
a. What number is 01101100 in base 10 ?
$\mathrm{e}=110=6$
$\mathrm{f}=0.1100=0.75$
$\mathrm{E}=\mathrm{e}-$ bias $=6-3=3$
$\mathrm{M}=1+\mathrm{f}=1+0.75=1.75$
sign bit $=0 \rightarrow$ positive
$1.75 \times 2^{3}=1.1100 \times 2^{3}=1110.0=14$
b. How would $3.3125(=3+5 / 16)$ be represented in eight-bit floating point?

$$
\begin{aligned}
& 3.3125=11.0101=1.10101 \times 2^{1} \\
& M=1.10101 \rightarrow f=0.10101 \\
& E=1 \rightarrow e=1+3=4=100 \\
& S=\text { positive }=0 \\
& 3.3125=010010101
\end{aligned}
$$

5. Give a value that makes each following expressions false, and explain why it makes the expression false. If there is no value for $x$ and $y$ that would make the expression false, indicate that. In each case, $x$ and $y$ are of type int.
a. $\left(\left(x^{\wedge} y\right)<0\right)$

If $x$ is $0 x 0, y$ is $0 x 0$
b. $((x \gg 31)+1)>=0$

This is always true. There's two cases: $x>=0$ or $x<0$. If $x>=0, x \gg 31$ is $0 x 0$.
$0 \times 0+1=0 x 00000001$. That's greater than 0 . If $x<0, x \gg 31$ is $0 \times 11111111$.
$0 x f f f f f f f f+1=0$. That's equal to 0 .
6. I have a C function with the following signature:
int practice_exam_problem(int a, int b);

Here is the assembly code for it:

```
<+0>:cmp %esi,%edi
<+2>: jle Ox4005be <practice_exam_problem+12>
<+4>: lea 0x5(%rsi,%rsi,1),%eax
<+8>: cmp %eax,%edi
<+10>: je 0x4005d4 <practice_exam_problem+34>
<+12>:cmp %esi,%edi
<+14>:jge 0x4005ca <practice_exam_problem+24>
<+16>:lea 0x4(%rdi,%rdi,2),%eax
<+20>:cmp %eax,%esi
<+22>: je Ox4005da <practice_exam_problem+40>
<+24>:cmp %esi,%edi
<+26>: jne 0x4005e0 <practice_exam_problem+46>
<+28>: mov $0x4,%eax
<+33>: retq
<+34>: mov $0x3,%eax
<+39>: retq
<+40>: mov $0xa,%eax
<+45>: retq
<+46>: mov $0x2,%eax
<+51>:retq
```

a. Give a value for parameters to make it return 2.

To return 2, we jump from <+26>, which triggers if \%esi != \%edi. A good way to get to <+26> is from <+14>, which jumps to <+24> iff \%edi >= \%esi. But we want to NOT trigger the jump on $<+10>$ checking if \%edi $==$ \%eax, where \%eax is 2 * \%rsi +5 .

Careful not to trigger the jumps on <+10> and <+2>!
For the path to work, these conditions must hold:
$\mathrm{a}<\mathrm{b}$
b ! $=3 a+4$

OR
$a>b$
$a!=2 b+5$
b. Give a value for parameters to make it return 3 .

The line that returns 3 is on <+34>. We jump to that from <+10>. That only happens when \%eax == \%edi. \%eax is 2 * \%rsi $+0 x 5$. So this returns three when 2* $\%$ rsi $+0 \times 5==\%$ edi.

So $a==2 b+5$.
c. Give a value for parameters to make it return 4.

Nothing jumps to <+28>, but <+14> jumps to <+24>, which is right before it. To get there, we need to jump from <+2>, the compare instruction behind <+14> So to make the jump to <+14> b <= a. To make the jump to <+24> a <= b. We want to avoid the jump to <+46>, so we want a == b. For all three conditions to hold true, we can just set $\mathrm{a}==\mathrm{b}$.
d. Give a value for parameters to make it return 10.

In order to return 10, we need to take the jump at <+22>, which happens when \%eax == \%esi. Before the comparison, \%eax is set to 3 * \%rdi +4 , which is $3 \mathrm{a}+$ 4; so we want $b==3 a+4$. We also want $\%$ edi < \%esi so we don't jump at <+14>. Finally, we load 2 * \%rsi + 5 into \%eax and compare that to \%edi; we don't want to take the jump, so we need $a!=2 b+5$.

Final restrictions:
$b==3 a+4$
a ! $=2 b+5$
$\mathrm{a}<\mathrm{b}$
7. Consider the following struct on an $x 86-64$ Linux machine:

```
struct my_struct {
        char a;
        long b;
        short c;
        float *d[2];
        unsigned char e[3];
        float f;
};
```

| 0x0 0x1 | 0x8 |  | $0 \times 10$ | 0x12 |
| :---: | :---: | :---: | :---: | :---: |
| a |  | b | C |  |
|  | 0x18 | 0x20 |  | 0x28 |
|  | $\mathrm{d}[0]$ |  | $\mathrm{d}[1]$ |  |


a. How many bytes will the struct occupy if our compiler optimizes for access time?

48 bytes
b. How many bytes will the struct occupy if our compiler optimizes for space?

34 bytes
8. Draw the stack frames of test and getbuf, given that the Instruction Pointer is currently at $0 \times 004017 c 7$ and the stack pointer is at $0 \times 5561 \mathrm{dcac}$ at the start of test. Indicate where the stack pointer is and the addresses and the content of the stack frames (variable names are ok).
C code:
void test() \{
int val;
val = getbuf();
printf("No exploit. Getbuf returned 0x\%x\n", val);
\}

```
unsigned getbuf() {
    char buf[BUFFER_SIZE];
    gets(buf);
    return 1;
}
```

Assembly Code:

| test: |  |  |
| :---: | :---: | :---: |
| 0x00401984 | sub | \$0x8,\%rsp |
| 0x00401988 | mov | \$0x0,\%eax |
| 0x0040198d | callq | 4017c3<getbuf> |
| 0x00401992 | mov | \%eax,\%edx |
| 0x00401994 | mov | \$0x4031d8,\%esi |
| 0x00401999 | mov | \$0x1,\%edi |
| 0x0040199e | mov | \$0x0,\%eax |
| 0x004019a3 | callq | 400e00[__printf_chk@plt](mailto:__printf_chk@plt) |
| 0x004019a8 | add | \$0x8,\%rsp |
| 0x004019ac | retq |  |
| getbuf: |  |  |
| 0x004017c3 | sub | \$0x28,\%rsp |
| 0x004017c7 | mov | \%rsp,\%rdi |
| 0x004017ca | callq | 401a4d <Gets> |
| 0x004017cf | mov | \$0x1,\%eax |
| 0x004017d4 | add | \$0x28,\%rsp |
| 0x004017d8 | retq |  |

Stack

|  | Address | Contents |
| :---: | :---: | :---: |
| $\begin{array}{r} \text { test } \\ \text { stack } \\ \text { frame } \end{array}$ | 0x5561dcac 0x5561dca4 0x5561dc9c | 0x401992 |
| getbuf stack frame | 0x5561dc94 <br> 0x5561dc8c <br> 0x5561dc84 <br> 0x5561dc7c <br> 0x5561dc74 |  |


| Instruction Pointer | $0 \times 004017 \mathrm{c7}$ |
| :---: | :---: |
| Stack Pointer | $0 \times 5561 \mathrm{dc} 74$ |

## /*

* anyOddBit - return 1 if any odd-numbered bit in word set to 1
* Examples anyOddBit(0x5) $=0$, anyOddBit(0x7) $=1$
* Legal ops: ! ~\&^|+ <<>>
* Max ops: 12
* Rating: 2
*/
int anyOddBit(int x) \{
int m8 = 0xAA;
int $\mathrm{m} 16=\mathrm{m} 8 \mid \mathrm{m} 8 \ll 8$;
int m32 $=\mathrm{m} 16 \mid \mathrm{m} 16 \ll 16$;
int oddx = x \& m32;
return !!oddx;
\}

